## CAT 2022 - Slot 1 Paper (Memory Based)

## Section 3 - Quantitative Aptitude

Q.1) Let $a$ and $b$ be natural numbers. If $a^{2}+a b+a=14$ and $b^{2}+a b+b=28$, then (2a+b) equals
(1) 10
(2) 7
(3) 8
(4) 9
Q.2) For any real number $x$, let $|x|$ be the largest integer less than or equal to $x$. If $\sum_{n=1}^{N}\left[\frac{1}{5}+\frac{n}{25}\right]=25$ then $N$ is
Q.3) Trains $A$ and $B$ start traveling at the same time towards each other with constant speeds from stations $X$ and $Y$, respectively. Train $A$ reaches station $Y$ in 10 minutes while train $B$ takes 9 minutes to reach station $X$ after meeting train $A$. Then the total time taken, in minutes, by train $B$ to travel from station $Y$ to station $X$ is
[1] 6
[2] 10
[3] 15
[4] 12
Q.4) A trapezium $A B C D$ has side $A D$ parallel to $B C, \angle B A D=90^{\circ}, B C=3 \mathrm{~cm}$ and $A D=8 \mathrm{~cm}$. If the perimeter of this trapezium is 36 cm , then its area, in sq. cm , is
Q.5) For natural numbers $x, y$, and $z$, if $x y+y z=19$ and $y z+x z=51$, then the minimum possible value of $x y z$ is
Q.6) Let $\mathrm{a}, \mathrm{b}, \mathrm{c}$ be non-zero real numbers such that $b^{2}<4 a c$, and $f(x)=a x^{2}+b c+c$. If the set S consists of all integers $m$ such that $f(m)<0$, then the set $S$ must necessarily be
[1] the empty set
[2] the set of all positive integers
[3] the set of all integers
[4] either the empty set or the set of all integers
Q.7) A mixture contains lemon juice and sugar syrup in equal proportion. If a new mixture is created by adding this mixture and sugar syrup in the ratio $1: 3$, then the ratio of lemon juice and sugar syrup in the new mixture is
[1] $1: 4$
2] $1: 5$
[3] $1: 6$
[4] $1: 7$
Q.8) The average of three integers is 13 . When a natural number $n$ is included, the average of these four integers remains an odd integer. The minimum possible value of $n$ is
[1] 3
[2] 1
[3] 4
[4] 5
Q.9) Amal buys 110 kg of syrup and 120 kg of juice, syrup being $20 \%$ less costly than juice, per kg . He sells 10 kg of syrup at $10 \%$ profit and 20 kg of juice at $20 \%$ profit. Mixing the remaining juice and syrup, Amal sells the mixture at ₹ 308.32 per kg and makes an overall profit of $64 \%$. Then, Amal's cost price for syrup, in rupees per kg , is
Q.10) For any natural number tt , suppose the sum of the first tt terms of an arithmetic progression is $\left(n+2 n^{2}\right)$. If the $n$ nh term of the progression is divisible by 9 , then the smallest possible value of $n$ is [1] 4
[2] 7
[3] 9
[4] 8
Q.11) Ankita buys 4 kg cashews, 14 kg peanuts and 6 kg almonds when the cost of 7 kg cashews is the same as that of 30 kg peanuts or 9 kg almonds. She mixes all the three nuts and marks a price for the mixture in order to make a profit of ₹ 1752 . She sells 4 kg of the mixture at this marked price and the remaining at a $20 \%$ discount on the marked price, thus making a total profit of ₹ 744 . Then the amount, in rupees, that she had spent in buying almonds is
[1] 1176
[2] 2520
[3] 1680
[4] 1440
Q.12) The average weight of students in a class increases by 600 gm when some new students join the class. If the average weight of the new students is 3 kg more than the average weight of the original students, then the ratio of the number of original students to the number of new students is
[1] $1: 2$
[2] $4: 1$
[3] $1: 4$
[4] $3: 1$
Q.13) The number of ways of distributing 20 identical balloons among 4 children such that each child gets some balloons but no child gets an odd number of balloons, is
Q.14) The largest real value of a for which the equation $|X+a|+|x-1|=2$ has an infinite number of solutions for x is
[1] 0
[2] 2
[3] 1
[4] -1
Q.15) All the vertices of a rectangle lie on a circle of radius $R$. If the perimeter of the rectangle is $P$, then the area of the rectangle is
[1] $\frac{P^{2}}{16}-R^{2}$
[2] $\frac{P^{2}}{2}-2 P R$
[3] $\frac{P^{2}}{8}-\frac{R^{2}}{2}$
[4] $\frac{P^{2}}{8}-2 R^{2}$
Q.16) Let $A B C D$ be a parallelogram such that the coordinates of its three vertices $A, B, C$ are (1, 1), (3, $4)$ and $(-2,8)$, respectively. Then, the coordinates of the vertex $D$ are
[1] $(-3,4)$
[2] $(0,11)$
$[3](4,5)$
[4] $(-4,5)$
Q.17) Let A be the largest positive integer that divides all the numbers of the form $3^{k}+4^{k}+5^{5}$ and B be the largest positive integer that divides all the numbers of the form $4^{k}+3\left(4^{k}\right)+4^{k+2}$, where $k$ is any positive integer. Then $(A+B)$ equals
Q.18) Let $0 \leq a \leq 100$ and $f(x)=|x-a|+|x-100|+|x-a-50|$. Then the maximum value of $f(x)$ becomes 100 when a is equal to
[1] 25
[2] 0
[3] 100
[4] 50
Q.19) Pinky is standing in a queue at a ticket counter. Suppose the ratio of the number of persons standing ahead of Pinky to the number of persons standing behind her in the queue is $3: 5$. If the total number of persons in the queue is less than 300 , then the maximum possible number of persons standing ahead of Pinky is
Q.20) In a class of 100 students, 73 like coffee, 80 like tea and 52 like lemonade. It may be possible that some students do not like any of these three drinks. Then the difference between the maximum and minimum possible number of students who like all the three drinks is
[1] 52
[2] 53
[3] 48
[4] 47
Q.21) Alex invested his savings in two parts. The simple interest earned on the first part at $15 \%$ per annum for 4 years is the same as the simple interest earned on the second part at $12 \%$ per annum for 3 years. Then, the percentage of his savings invested in the first part is
[1] 37.5\%
[2] 60\%
[3] 62.5\%

## Learn( $\theta$ )

[4] $40 \%$
Q.22) In a village, the ratio of number of males to females is $5: 4$. The ratio of number of literate males to literate females is $2: 3$. The ratio of the number of illiterate males to illiterate females is 4 : 3. If 3600 males in the village are literate, then the total number of females in the village is

| Q.No. | Quant |
| :---: | :---: |
| 1 | 3 |
| 2 | 44 |
| 3 | 3 |
| 4 | 66 |
| 5 | 34 |
| 6 | 4 |
| 7 | 4 |
| 8 | 4 |
| 9 | 160 |
| 10 | 2 |
| 11 | 3 |
| 12 | 2 |
| 13 | 84 |
| 14 | 3 |
| 15 | 4 |
| 16 | 4 |
| 17 | 82 |
| 18 | 4 |
| 19 | 111 |
| 20 | 4 |
| 21 | 1 |
| 22 | 43200 |

